

Depth-Based Image Registration

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ABSTRACT

Image registration is a fundamental task in computer vision because it can significantly contribute to high-level computer vision and benefit numerous practical applications. Though a lot of image registration techniques exist in literature, there is still a significant amount of research to be conducted because there are a lot of issues that need to be solved such as the parallax problem. The traditional image registration algorithms suffer from the parallax problem due to their underlying assumption that the scene can be regarded approximately planar which is not satisfied in the case of large depth variation in the images with high-rise objects. With regard to the parallax problem, a new strategy is proposed by leveraging the depth information via 3D reconstruction. One novel idea is to recover the depth in the image region with high-rise objects to build accurate transform function for image registration. Our method mitigates the parallax problem and can achieve robust registration results, which is validated by our experiments. Our algorithm is attractive to numerous practical applications.

Keywords: 3D reconstruction, image registration, depth estimation, parallax problem

1. INTRODUCTION

Image registration is a fundamental task in image processing and computer vision which matches two or more images taken at different times and different viewpoints, by geometrically aligning reference and sensed images. There has been a broad range of techniques developed over the years in literature. A comprehensive survey of image registration methods was published in 1992 by Brown,¹ including many classic methods still in use. Due to the rapid development of image acquisition devices, more image registration techniques emerged afterwards and were covered in another survey² published in 2003. Different applications due to distinct image acquisition require different image registration techniques. In general, manners of the image acquisition can be divided into three main groups:

- *Different viewpoints (multiview analysis)*. Images of the same scene are acquired from different viewpoints. The aim is to gain a larger 2D view or a 3D representation of the scanned scene.
- *Different times*. Images of the same scene are acquired at different times, often on regular basis, and possibly under different conditions. The aim is to find and evaluate changes in the scene which appeared between the consecutive image acquisitions.
- *Different sensors*. Images of the same scene are acquired by different sensors. The aim is to integrate the information obtained from different source streams to gain more complex and detailed scene representation.

Due to the diversity of images to be registered and various types of degradations, it is impossible to design a universal method applicable to all registration tasks. Every method should take into account not only the assumed type of geometric deformation between the images but also the radiometric deformations and noise corruption, required registration accuracy and application-dependent data characteristics. Nevertheless, the majority of the registration methods consists of the following four steps: feature detection, feature matching, transform model estimation, image resampling and transformation.

A widely used feature detection method is corner detection. Kitchen and Rosenfeld³ proposed to exploit the second-order partial derivatives of the image function for corner detection. Dreschler and Nagel⁴ searched for the local extrema of the Gaussian curvature. However, corner detectors based on the second-order derivatives of the image function are sensitive to noise. Thus Forstner⁵ developed a more robust, although time consuming, corner detector, which is based on the first-order derivatives only. The reputable Harris detector⁶ also uses first-order derivatives for corner detection.

Feature matching includes area-based matching and feature-based matching. Classical area-based method is cross-correlation (CC)⁷ exploit for matching image intensities directly. For feature-based matching, Goshtasby⁸ described the registration based on the graph matching algorithm. Clustering technique, presented by Stockman et al.,⁹ tries to match points connected by abstract edges or line segments.

After the feature correspondence has been established the mapping function is constructed. The mapping function should transform the sensed image to overlay it over the reference image.

Finally interpolation methods such as nearest neighbor function, bilinear, and bicubic functions are applied to the output of the registered images.

The prevailing image registration methods, such as the algorithm of Davis and Keck,^{10,11} assume all the feature points are coplanar and build a homography transform matrix to do registration. The advantage is that they have low computational cost and can handle planar scenes conveniently; however, with the assumption that the scenes are approximately planar, they are inappropriate in the registration applications when the images have large depth variation due to the high-rise objects, known as the parallax problem. Parallax is an apparent displacement of difference of orientation of an object viewed along two different lines of sight, and is measured by the angle or semi-angle of inclination between those two lines. Nearby objects have a larger parallax than further objects when observed from different positions. Therefore, as the viewpoint moves side to side, the objects in the distance appear to move slower than the objects close to camera.

In this paper, we propose a depth based image registration algorithm by leveraging the depth information. Our method can mitigate the parallax problem caused by high-rise scenes in the images by building accurate transform function between corresponding feature points in multiple images. Given an image sequence, we first select a number of feature points and then match the features in all images. Then we estimate the depth of each feature point from feature correspondences. With the depth information, we can project the image in 3D instead of using a homography transform. Further more, fast and robust image registration algorithm can be achieved by combining the traditional image registration algorithms and depth based image registration method proposed in this paper. The idea is that we first compute the 3D structure of a sparse feature points set and then divide the scene geometrically into several approximately planar regions. For each region, we can perform a depth based image registration. Accordingly, robust image registration is achieved.

The remainder of this paper is organized as follows. Section 2 presents the 3D reconstruction algorithm on which our experiments are based. In Section 3, we describe our depth-based image registration algorithm from theoretical aspects to explain why it can mitigate the parallax problem. Section 4 compares our algorithm with the algorithm of Davis and Keck¹⁰ on the same video sequence. We conclude the paper in Section 5.

2. 3D RECONSTRUCTION FROM VIDEO SEQUENCES

Here, we simply introduce the 3D reconstruction algorithm proposed in Ma et. al's book¹² on which our experiments are based. When developing a stereo vision algorithm for registration, the requirements for accuracy vary from those of standard stereo algorithms used for 3D reconstruction. For example, a multi-pixel disparity error in an area of low texture, such as a white wall, will result in significantly less intensity error in the registered image than the same disparity error in a highly textured area. In particular, edges and straight lines in the scene need to be rendered correctly.

The 3D reconstruction algorithm is implemented using the following steps.¹² First, geometric features are detected automatically in each individual images. Secondly, feature correspondence is established across all the images. Then the camera motion is retrieved and the camera is calibrated. Finally the Euclidean structure of the scene is recovered.

2.1. Feature selection

The first step in 3D reconstruction is to select candidate features in all images for tracking across different views. Ma et al.¹² use point feature in reconstruction which is measured by Harris' criterion,

$$C(\mathbf{x}) = \det(G) + k \times \text{trace}^2(G), \quad (1)$$

where $\mathbf{x} = [x, y]^T$ is a candidate feature, $C(\mathbf{x})$ is the quality of the feature, k is a pre-chosen constant parameter and G is a 2×2 matrix that depends on \mathbf{x} , given by

$$G = \begin{bmatrix} \sum_{W(\mathbf{x})} I_x^2 & \sum_{W(\mathbf{x})} I_x I_y \\ \sum_{W(\mathbf{x})} I_x I_y & \sum_{W(\mathbf{x})} I_y^2 \end{bmatrix} \quad (2)$$

where $W(\mathbf{x})$ is a rectangular window centered at \mathbf{x} and I_x and I_y are the gradients along the x and y directions which can be obtained by convolving the image I with the derivatives of a pair of Gaussian filters. The size of the window can be decided by the designer, for example 7×7 . If $C(\mathbf{x})$ exceeds a certain threshold, then the point \mathbf{x} is selected as a candidate point feature.

2.2. Feature correspondence

Once the candidate point features are selected, the next step is to match them across all the images. In this subsection, we use a simple feature tracking algorithm based on a translational model.

We use the sum of squared differences (SSD)¹³ as the measurement of the similarity of two point features. Then the correspondence problem becomes looking for the displacement \mathbf{d} that satisfies the following optimization problem:

$$\min_{\mathbf{d}} \doteq \sum_{\mathbf{x} \in W(\mathbf{x})} [I_2(\mathbf{x} + \mathbf{d}) - I_1(\mathbf{x})]^2 \quad (3)$$

where \mathbf{d} is the displacement of a point feature of coordinates \mathbf{x} between two consecutive frames I_1 and I_2 . Lucas and Kanade also give the close form solution of 3

$$\mathbf{d} = -G^{-1}\mathbf{b} \quad (4)$$

where

$$\mathbf{b} \doteq \begin{bmatrix} \sum_{W(\mathbf{x})} I_x I_t \\ \sum_{W(\mathbf{x})} I_y I_t \end{bmatrix} \quad (5)$$

G is the same matrix we used to compute the quality of the candidate point feature in Eq. 1, and $I_t \doteq I_2 - I_1$.

2.3. Estimation of camera motion parameters

In this subsection, we recover the projective structure of the scene from the established feature correspondence. We will follow the notation used in Ma et al.'s book.¹² For the detail of the proof of this algorithm, please refer to the reference.

The reconstruction algorithm is based on a perspective projection model with a pinhole camera. Suppose we have a generic point $p \in \mathbb{E}^3$ with coordinates $\mathbf{X} = [X, Y, Z, 1]^T$ relative to a world coordinate frame. Given two frames of one scene which is related by a motion $g = (R, T)$, the two image projection point \mathbf{x}_1 and \mathbf{x}_2 are related as follows:

$$\lambda_1 \mathbf{x}'_1 = \Pi_1 \mathbf{X}_p, \quad \lambda_2 \mathbf{x}'_2 = \Pi_2 \mathbf{X}_p, \quad (6)$$

where $\mathbf{x}' = [x, y, 1]^T$ is measured in pixels, λ_1 and λ_2 are the depth scale of \mathbf{x}_1 and \mathbf{x}_2 , $\Pi_1 = [K, 0]$ and $\Pi_2 = [KR, KT]$ are the camera projection matrices and K is the camera calibration matrix. In order to estimate λ_1 , λ_2 , Π_1 and Π_2 , we need to introduce the epipolar constraint. From Eq. 6, we have

$$\mathbf{x}'_2{}^T K^{-T} \hat{T} R K^{-1} \mathbf{x}'_1 = 0. \quad (7)$$

The fundamental matrix is defined as:

$$F \doteq K^{-T} \hat{T} R K^{-1}. \quad (8)$$

With the above model, we could estimate the fundamental matrix F via the Eight-point algorithm.¹² Then we could decompose the fundamental matrix to recover the projection matrices Π_1 and Π_2 and the 3D structure. We only give the solution here by canonical decomposition:

$$\Pi_1 p = [I, 0], \Pi_2 p = [(\hat{T}')^T F, T'], \lambda_1 \mathbf{x}'_1 = \mathbf{X}_p, \lambda_2 \mathbf{x}'_2 = (\hat{T}')^T F \mathbf{X}_p + T'. \quad (9)$$

Table 1. Eight-point algorithm

Given a set of initial point feature correspondences expressed in pixel coordinates $(\mathbf{x}'_1, \mathbf{x}'_2)$ for $j = 1, 2, \dots, n$:

• **A first approximation of the fundamental matrix:** Construct the matrix $\chi \in \mathbb{R}^{n \times 9}$ from the transformed correspondences $\tilde{\mathbf{x}}_1^j \doteq [\tilde{x}_1^j, \tilde{y}_1^j, 1]^T$ and $\tilde{\mathbf{x}}_2^j \doteq [\tilde{x}_2^j, \tilde{y}_2^j, 1]^T$, where the j th row of χ is given by $[\tilde{x}_1^j \tilde{x}_2^j, \tilde{x}_1^j \tilde{y}_2^j, \tilde{x}_1^j \tilde{x}_2^j, \tilde{y}_1^j \tilde{x}_2^j, \tilde{y}_1^j \tilde{y}_2^j, \tilde{y}_1^j \tilde{y}_2^j, \tilde{y}_1^j, \tilde{x}_2^j, \tilde{y}_2^j, 1]^T \in \mathbb{R}^9$. Find the vector $F^s \in \mathbb{R}^9$ of unit length such that $\|\chi F^s\|$ is minimized as follows: Compute the singular value decomposition (SVD) of $\chi = U\Sigma V^T$ and define F^s to be the ninth column of V . Unstack the nine elements of F^s into a square 3×3 matrix \tilde{F} .

• **Imposing the rank-2 constraint:** Compute the SVD of the matrix F recovered from data to be $\tilde{F} = U_F \text{diag}\{\sigma_1, \sigma_2, \sigma_3\} V_F^T$. Impose the rank-2 constraint by letting $\sigma_3 = 0$ and reset the fundamental matrix to be $F = U_F \text{diag}\{\sigma_1, \sigma_2, 0\} V_F^T$.

2.4. Depth estimation

The Euclidean structure \mathbf{X}_e is related to the projective reconstruction \mathbf{X}_p by a linear transform $H \in \mathbb{R}^{4 \times 4}$,

$$\Pi_{ip} \sim \Pi_{ie} H^{-1}, \mathbf{X}_p \sim H \mathbf{X}_e, i = 1, 2, \dots, m, \quad (10)$$

where \sim means equality up to a scale factor and

$$H = \begin{bmatrix} K_1 & 0 \\ -\nu^T K_1 & 1 \end{bmatrix} \in \mathbb{R}^{4 \times 4}. \quad (11)$$

With the assumption that K is constant, we could estimate the unknowns K and ν with a gradient decent optimization algorithm. In order to obtain a unique solution, we also assume that the scene is generic and the camera motion is rich enough.

Fig. 1 shows the first frame and the 88th frame of the test video sequence ‘oldhousing’. In our experiment, we will register all the frames in the video sequence to the first frame. Fig. 2 show the selected feature points on the first frame which are used for camera pose estimation. Fig. 3 show the estimated depth map of the selected feature points and the camera pose.



(a) The 1st frame in the ‘oldhousing’ video sequence

(b) The 88th frame in the ‘oldhousing’ video sequence

Figure 1. Original frames used for image registration

3. IMAGE REGISTRATION WITH DEPTH INFORMATION

Once we obtain the 3D structure of the feature points, the motion, and calibration of the camera, we can start to register the rest of the pixels in the images with the estimated depth information. The traditional image registration algorithms,



Figure 2. The feature points selected for depth estimation on the 1st frame.

such as the algorithm of Davis and Keck,^{10,11} try to register the two images by computing the homography matrix H between corresponding feature points. The limit of this algorithm is that they assume all the points in the physical world are coplanar or approximately coplanar, which is not true with high-rise scenes. In order to mitigate this problem, we propose a novel algorithm which first segment the image geometrically and then perform the registration to each region with depth estimation.

3.1. Geometrical segmentation

In order to perform the geometrical segmentation, the most intuitive method is to obtain the dense surface model of the scene and then segment the surface into several regions based on the depth of the points. However, we need to know the correspondence for almost all the pixels to compute the dense surface model, which means we need to know all the pixel correspondence before the registration. In order to avoid this dilemma, we will not use the traditional 3D reconstruction algorithm to estimate the dense surface model. Instead, we directly segment the scene into several regions by clustering the sparse 3D points set that we obtained in Section 2. With the assumption that each segment region of the scene is approximately coplanar in the physical world, we could easily estimate the plane model and project the 3D plane onto the image frames. Comparing the assumption that the whole scene is coplanar in the physical world used in the traditional image registration algorithms, this assumption is valid in most circumstances.

There are a lot of algorithms for data clustering. The most famous hard-clustering algorithm is k-means.¹⁴ The k-means algorithm assigns each data point to the cluster whose centroid is nearest. Here, we use the distance to a 3D plane in the physical world as the measurement. For each cluster, we could choose the plane that has the smallest sum of distance of all the data points in the cluster.

3.2. Depth estimation

Here, we only consider two images. Suppose for the first image, we have the 3D point set $\mathbf{X}_e^j, j = 1, 2, \dots, n$ which could be divided into three clusters, $\mathbf{X}_{e1}, \mathbf{X}_{e2}, \mathbf{X}_{e3}$. For each cluster, there are at least three non-collinear points. Then we could have the plane model for this cluster. Let's take the example of \mathbf{X}_{e1} , suppose there are m points in the cluster and we have the plane model as follows:

$$\mathbf{A} \cdot \mathbf{p} = 1. \quad (12)$$

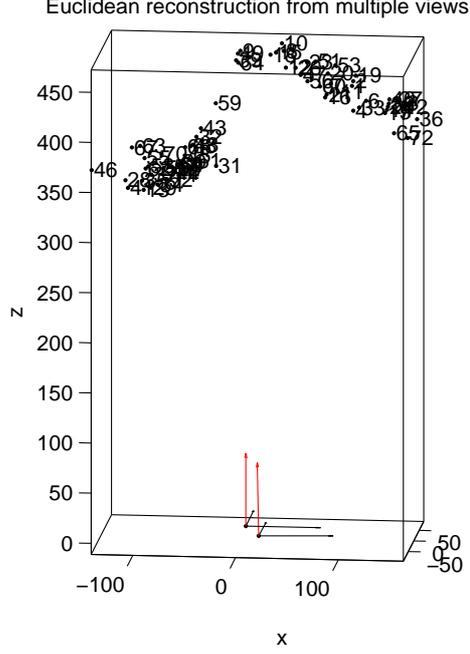


Figure 3. The estimated depth map and camera pose for the selected feature points of the 1st and 88th frames.

where $\mathbf{A} = [\mathbf{X}_{e1}^i]$, $i = 1, \dots, m$ and $p = [a, b, c]^T$ is the plane parameter.

Given an arbitrary point $\mathbf{x}^i = [x^i, y^i]^T$ measured in pixels in the first cluster, we could estimate its depth scale λ^i by solving the following equation.

$$\lambda^i \mathbf{x}^i = H_1^{-1} \Pi_1 \mathbf{X}_e^i. \quad (13)$$

where $\mathbf{x}^i = [x^i, y^i, 1]^T$, H_1^{-1} and Π_1 are estimated in Section 2. In Eq. 13, only λ^i is unknown and with the constraint on \mathbf{X}_e^i with Eq. 12, we could easily get the value of λ^i .

Then, with $\Pi_1 = [I, 0]$, we could have $X_p^i = [\lambda^i x^i, \lambda^i y^i, \lambda^i, 1]$. from Eq. 6, we can get the relation between two image projection point \mathbf{x}_1^i and \mathbf{x}_2^i as follows:

$$\widehat{\mathbf{x}}_2^{i'} = \Pi_2 \mathbf{X}_p^i. \quad (14)$$

where $\widehat{\mathbf{x}}_2^{i'} = [\lambda_2^i x_2^i, \lambda_2^i y_2^i, \lambda_2^i]$. We could then get the position of the corresponding point $\mathbf{x}_2^i = [x_2^i, y_2^i]$ in the second image.

4. EXPERIMENTAL RESULTS

The data includes a sequence of 88 images captured from one camera. We first select 72 feature points in the first image and then find the corresponding feature points in the rest of the images. The depth estimates of these points are calculated by the algorithm introduced in Section 2.

In our experiment, we regard the first image's local coordinate system as world coordinate system so the first image can be viewed as a reference image. Then the rest of the images are registered to the reference image. We also applied the algorithm of Davis and Keck¹⁰ to accomplish the same task for comparison purpose.

Fig. 1 is the 1st frame and the 88th frame in the test image sequence. Fig. 4 is the registration result using our algorithm and Fig. 5 is the output of the algorithm of Davis and Keck.¹⁰ Fig. 6 shows the difference image between the registered image and the first image using our algorithm and Fig. 7 shows the difference image from the algorithm of Davis and Keck.¹⁰ We can see that our result can mitigate the parallax problem since the roof and wall corners are registered



Figure 4. Our algorithm test result, in which the 88th frame is registered to the 1st frame.



Figure 5. The test result under the algorithm of Davis and Keck, in which the 88th frame is registered to the 1st frame.

correctly; on the contrary, the registered image by the algorithm of Davis and Keck¹⁰ has a lot of artifacts caused by the parallax problem. We also show some registration results using our algorithm in Fig. 8~ Fig. 9.

In order to further compare our algorithm to the algorithm of Davis and Keck, we compute the root of mean squared errors (RMSE) of the registration results from both algorithms. Fig. 10 shows that the registration error of our algorithm is less than 50% than that of the algorithm of Davis and Keck.

The result shows that our image registration algorithm can mitigate the parallax problem because most of the scene is registered without vibration, as opposed to registration results under the algorithm of Davis and Keck in which the high-rise scene in the sensed images significantly moved after registration to the reference images. The reason is that the algorithm of Davis and Keck assumes all the points in the images are coplanar. While this assumption is satisfied when the distance between the camera and the interested scene is so large that the small depth variation can be neglected, it fails in the case



Figure 6. The difference image between the registered 88th image (using our algorithm) and the 1st image.

of high-rise scene. Therefore, depth information should be used to accomplish the registration for this specific high-rise region of the images.

Finally, we would like to point out that the algorithm of Davis and Keck¹⁰ assumes a planar registration. Their scheme was designed for use with high-altitude aerial imagery where planar transformations are fairly good approximations. Furthermore, their scheme uses RANSAC to remove poor matching points during the computation. This can help to deal with some depth discontinuities that may be present in the high-altitude aerial images. In our experiments, the test images contain salient 3D scenes; these images are out of the domain for the algorithm of Davis and Keck. This is the reason why the algorithm of Davis and Keck does not perform well.

5. CONCLUSION

In this paper, we propose a new 2D image registration method by leveraging depth information. While traditional image registration algorithms fail to register high-rise scene accurately because the points cannot be assumed to be simply planar, our image registration algorithm can mitigate the parallax problem.

Our future works include:

- Develop a robust 3D model based on the state-of-the-art depth estimate algorithm^{15,16} given a video sequence. The reliability of the depth estimates is crucial to depth-based registration algorithm; therefore, the highly robust 3D reconstruction technique is required to implement our algorithm. Up to now, most recent depth recovery algorithms reported in the literature claim to recover consistent depth from some challenging video sequences^{15,16}. We can apply or modify this state-of-the-art depth map recovery method to develop depth-based image registration algorithm.
- Combine depth-based image registration method with traditional algorithms. In other words, we can use depth information to register high-rise region while applying traditional registration algorithm for other planar region of the image. The purpose is to tradeoff between the accuracy of the registration and the high computational cost introduced by 3D reconstruction. The combined algorithm thus can enjoy both the high efficiency of the traditional algorithm and the high robustness of the depth-based registration method.



Figure 7. The difference image between the registered 88th image (using the algorithm of Davis and Keck) and the 1st image.

- We would use our depth-based image registration algorithm in practical applications to further verify the performance of our algorithm compared to the traditional ones.

Disclaimers

The views and conclusions contained herein are those of the authors and should not be interpreted as necessarily representing the official policies or endorsements, either expressed or implied, of AFRL or the U.S. Government.

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Figure 8. The 37th frame in the ‘oldhousing’ video sequence.

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Figure 9. Our algorithm test result, in which the 37th frame is registered to the 1st frame.

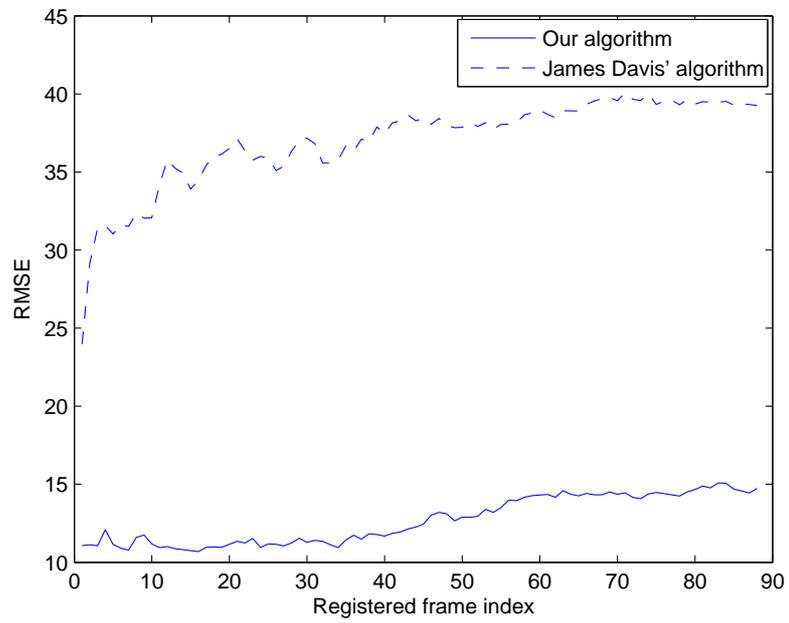


Figure 10. Our algorithm test result comparing to that under the algorithm of Davis and Keck, in which all the 88 frames are registered to the 1st frame.